

Volumetric Filtering for Shot Gather Interpolation in Swath Seismic Acquisition

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Abstract—Due to environmental and economic constraints inherent to seismic exploration, there are often missing shotpoints and receivers that degrade the resolution of the final seismic image. Hence, sophisticated interpolation techniques are required for the recovery of dense and uniform spatial sampling. Recent approaches improve the interpolation by adopting robust models through denoisers. We introduce a 3-D shot gather interpolation method that jointly considers a sparse prior and a regularization induced by a multichannel volumetric denoiser. The proposed volumetric regularization uses collaborative filters that perform denoising through transform-domain shrinkage of a group of similar seismic cubes extracted from a land seismic acquisition. This grouping and collaborative filtering paradigm exploit the local correlation present in each cube and the nonlocal correlation between different cubes. Experiments on the *Stratton 3-D survey* show that the proposed method can interpolate 3-D shot gathers in an orthogonal seismic recording from a swath geometry, outperforming methods based on 2-D denoisers and 5-D seismic data reconstruction in terms of root mean square error and the recovery of seismic reflections.

Index Terms—BM4D, denoiser prior, plug and play (PnP) denoiser, seismic acquisition, shot data reconstruction, swath geometry.

I. INTRODUCTION

REGULAR sampling plays an important role in seismic data processing and impacts the imaging quality and interpretation of hydrocarbon exploration. Nevertheless, the sampled seismic data is often incomplete or irregular due to environmental, topographic, or social constraints [1]. Therefore, the missing information must be recovered or interpolated to obtain the regular seismic data. Several reconstruction algorithms are designed for receiver [2], [3] and shot gather recovery [4], [5], [6] under the assumption that seismic data enjoys an approximate sparse representation with respect to a particular transform or dictionary, such as curvelets, seislets,

and atom waves [7]. The reconstruction is further impaired by the random and seismic ambient noise of the acquisition [1], [8]. To improve the interpolation of the seismic data, [9] complements the sparse representation with an implicit data prior implemented as a denoising algorithm under the consensus equilibrium (CE) framework [10].

All the above methods for shot gather interpolation have been applied on geometries with a line of shotpoints and a line of receivers, such as the cross-spread, split-spread, and full-spread geometries [5]. In particular, the cross-spread is often used for shot-gather interpolation experiments, where the information can be analyzed with high correlation and where sparsity is satisfied [4], [9]. However, land 3-D acquisition commonly is carried out by swath shooting [11], [12], [13] in which receiver cables are laid out in parallel lines and shots are positioned in a perpendicular direction [14], and all geophones simultaneously record the elastic energy emitted by a source [15] resulting in a 3-D shot gather. Therefore, in this case, previous 2-D shot gather interpolation methods cannot account for the 3-D structure of the acquired seismic waveform in a missing shot gather. Even though higher-dimensional methods exist [3], [16], [17], these have thus far been considered for interpolating missing receivers and not for the interpolation of full 3-D shot gathers.

We introduce a 3-D shot-gather interpolation method that employs a multidimensional regularization model through a volumetric denoiser. Specifically, the denoiser employs the grouping and collaborative filtering paradigm where similar 3-D seismic cubes are stacked in a 4-D tensor and jointly filtered in a transform domain. This transformation exploits the local correlation present in each cube and the nonlocal correlation between different cubes leading to an improved separation of signal and noise that cannot be attained by 2-D denoisers. We explore the proposed method in a realistic swath seismic acquisition survey where we further leverage the similarity of multiple channels (3-D shot gathers) to perform the grouping of the seismic cubes. Numerical results show the improvement in speed and accuracy when compared with interpolation methods that employ 2-D denoisers as a regularizer block-matching and 3-D filtering-CE (BM3D-CE) and the 5-D interpolation (5D-DRR) using the optimally damped rank-reduction method [17].

II. ACQUISITION MODEL USING SWATH GEOMETRY

A cross-spread configuration consists of a shot line orthogonally intercepted by a receiver line [Fig. 1(a)], resulting in

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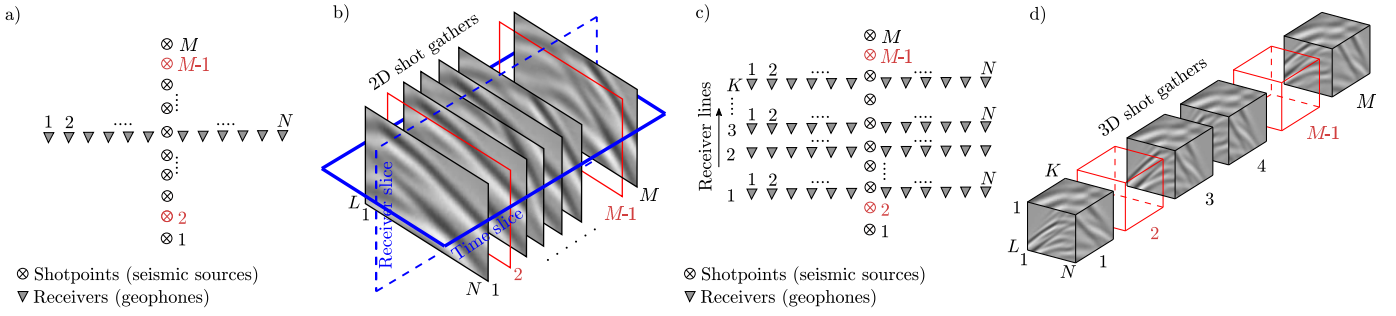


Fig. 1. (a) Cross-spread [4], [9] and (c) swath geometry [12]. (b) and (d) Three-dimensional and 4-D tensor presentation for the subsampled acquisitions from (a) and (c), respectively, by removing the shotpoints at 2 and $M - 1$.

a 3-D seismic survey as shown in Fig. 1(b) composed by M stacked 2-D shot gathers. However, in practice, the seismic acquisition is performing juxtaposition of cross-spreads [15]. Hence, recording the seismic signal for a shot employs several lines of receivers simultaneously in a multiorthogonal seismic acquisition called swath geometry [12], as illustrated in Fig. 1(c). Therefore, in this case, the seismic data can be represented as 4-D structures comprising L samples in time of the reflected energy emitted by M shot gathers, captured by a sequence of K receiver lines with N receivers per line. Here, a single shot gather is recorded by an $L \times N \times K$ array as shown in Fig. 1(d). Additionally, swath geometry preserves the advantages of a cross-spread and provides seismic signals with less random noise [4].

The acquisition process illustrated in Fig. 1(c) can be modeled as a system of linear equations given by the following equation:

$$\mathbf{y} = \Phi \mathbf{x} + \omega, \quad (1)$$

where $\Phi \in \mathbb{R}^{LNK(M-k) \times LNK M}$ is the acquisition operator, $\mathbf{x} \in \mathbb{R}^{LNK M}$ is the vector representation of the M 3-D shot gathers in Fig. 1(d), and ω accounts for the acquisition noise. $\Phi \in \mathbb{R}^{LNK(M-k) \times LNK M}$ is defined as $\Phi = \mathbf{S} \otimes \mathbf{I}_{LNK}$, where $\otimes$ represents the Kronecker product [18], $\mathbf{I}_{LNK}$ is an $LNK \times LNK$ identity matrix, $\mathbf{S} \in \mathbb{R}^{M-k \times M}$ model the shot subsampling effect and is obtained by removing from the identity matrix $\mathbf{I}_M$, and k rows corresponding to the k missing shot gathers. The acquired shot gathers $\mathbf{y}$ are then used to estimate the whole dataset $\mathbf{x}$.

III. VOLUMETRIC SHOT-GATHER INTERPOLATION

For the estimation, the traditional compressive sensing (CS) formulation exploits the sparse representation of $\mathbf{x}$ on a given transform basis $\mathbf{D} \in \mathbb{R}^{LNK M \times LNK M}$ such as wavelets or curvelets [19], with the estimate $\hat{\mathbf{x}}$ of $\mathbf{x}$ defined as the solution of

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \Phi \mathbf{x}\|_2^2 + \lambda \|\mathbf{D} \mathbf{x}\|_1, \quad (2)$$

where the parameter $\lambda > 0$ balances the quadratic fidelity versus the ℓ_1 sparsity penalty.

Although the sparsity promoted with the ℓ_1 -norm has been widely used in seismic applications [4], [5], a recent work [9] explored combining sparsity and plug-and-play (PnP) priors to improve the reconstruction. PnP priors have been studied as a

mechanism for incorporating image denoisers as implicit regularizations for inverse problems [20], [21]. The interpolated seismic data in [9] is the solution to the following optimization problem:

$$\hat{\mathbf{x}} = \arg \min_{\mathbf{x}} \frac{1}{2} \|\mathbf{y} - \Phi \mathbf{x}\|_2^2 + \lambda \|\mathbf{D} \mathbf{x}\|_1 + \beta h(\mathbf{x}), \quad (3)$$

where λ and β are regularization parameters and h is the implicit PnP regularization function defined by the BM3D denoiser. However, since BM3D is a 2-D denoiser, the regularization defined by BM3D is applied through 2-D structures of the seismic data cube, and, therefore, as a PnP prior, it cannot take full advantage of the higher dimensional structure of the seismic waveform (i.e., the multiples cubes in Fig. 1(d) correspond to a 4-D tensor acquired in a swath acquisition geometry).

Here, we propose to interpolate missing shot gathers of the target (preplot) swath geometry in land seismic acquisitions using (3) and the *volumetric multichannel BM4D denoiser* [22], [23] as PnP prior instead of BM3D. Similar to [9], we address (3) using the *CE approach* [10], [24] that solves a generalized inverse problem that includes multiple data fitting and regularization terms. Within CE, we use BM4D iteratively on an auxiliary variable $\mathbf{v}_k$ to pull the current estimate $\hat{\mathbf{x}}_k$ toward a solution $\hat{\mathbf{x}}$ with improved regularity of similar seismic structures along the M 3-D shot gathers. In the following, we present in detail the *multichannel denoising algorithm in the context of multiple receiver lines acquisition*.

A. Collaborative Filtering of Volumetric Multichannel Data

1) *Noise Model*: The input $\mathbf{v}_k$ of the denoiser is multi-channel volumetric (i.e., 4-D) data structured as in Fig. 1(d). Specifically, we model $\mathbf{v}_k$ as a noisy realization of $\mathbf{x}$

$$\mathbf{v}_k = \mathbf{x} + \mathbf{n}_k, \quad \mathbf{n}_k(\cdot) \sim \mathcal{N}(0, \sigma_k^2), \quad (4)$$

where $\mathbf{n}_k$ is zero-mean i.i.d. Gaussian noise with variance σ_k^2 . The goal of the filtering is then to estimate $\mathbf{x}$ from $\mathbf{v}_k$.

2) *Multichannel BM4D Filtering*: The land seismic acquisition is performed by a swath shooting sequence over a multiorthogonal geometry, which consists of all receivers that are actively recording for a given shot point [15]. Due to the parallel nature of receiver lines within a swath geometry, shot gathers capture waveform shapes and seismic signal structures that repeat in the majority of the records such as reflection

hyperbolas, ground roll waves (surface waves), and refraction (linear events). Therefore, there are similar structures between the different seismic shots, which are exploited to use algorithms that can find those areas of high similarities, such as BM4D. We adopt directly the BM4D implementation of [23] applied as a multichannel denoiser across principal components PCs computed across the shot gathers, extending the 2-D multichannel approach of [25] to 4-D data.

We begin the denoising by *computing the PC* across the M 3-D shot gathers that form $\mathbf{v}_k$, resulting in M 3-D PCs, which we regard as the channels for BM4D denoising. BM4D processes the data in groups of small $4 \times 4 \times 4$ cubes extracted from the individual channels according to the following scheme.

The first PC has the highest signal-to-noise ratio among the PCs and $\mathbf{v}_k$. Hence, we select this channel to evaluate *cube-matching*, identifying volumetric positions of similar cubes. Then, individually for each channel, we build groups of similar cubes collected from the positions indicated by the cube-matching, as illustrated in Fig. 2. Each group of cubes is organized into a 4-D structure by stacking the cubes along a nonlocal fourth dimension. As the common broader structures persist across the channels, also the groups built for channels other than the first one enjoy high internal self-similarity.

We *transform* each group of cubes, obtaining 4-D spectra in which the underlying regular structures are extremely sparsely represented because of self-similarity between the grouped cubes. Due to this sparsity, by *shrinkage* of the 4-D spectra, we attenuate the noise while preserving most of the underlying signal and enhancing both local and nonlocal regularity across the multiple channels.

After shrinkage, the 4-D group transform is *inverted*, and each resulting cube estimate is *aggregated* into the corresponding channel at its original position. In this way, we form a denoised estimate of the M channels.

Finally, the *inverse principal component analysis (PCA)* with respect to the M channels returns a denoised estimate of the M 3-D shot gathers.

Note that the above denoising procedure operates across five dimensions, decorrelating the 4-D data [as shown in Fig. 1(d)] through a data-driven 5-D highly redundant transform resulting from PCA and group-wise 4-D transforms. The extra dimension corresponds to the nonlocal dimension along which we encode the similarity of grouped blocks.

IV. SIMULATIONS AND RESULTS

The experiments to evaluate the proposed volumetric denoising regularization for shot-gather interpolation were performed using the *Stratton 3-D survey* [26], specifically using a Swath corresponding to source line 556. The data acquisition consists of a multiorthogonal land seismic survey in the south of Texas. The swath acquisition parameters are: $M = 10$ 3-D shot gathers, $K = 6$ receiver lines with $N = 112$ receivers, and $L = 500$ time samples. We simulate $k = 3$ missing shotpoints at positions 4, 6, 9 and initialize the missing shot gathers as zero. We used the 3-D wavelet transform symlet-8 as dictionary $\mathbf{D}$ for the sparse representation used in (3). The 3-D wavelet transform is applied in the receiver line

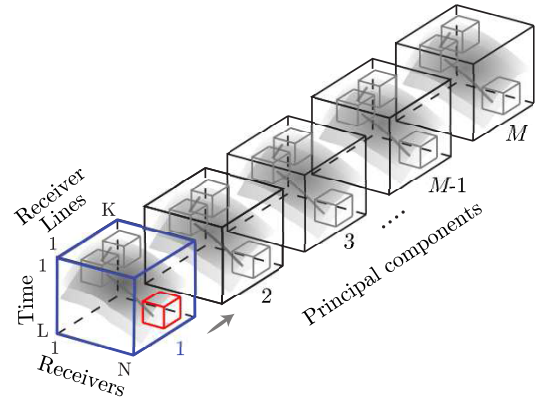


Fig. 2. Illustration of multichannel BM4D cube-matching for different PCs of $\mathbf{v}_k$, showing the matching of three cubes. The cube-matching is performed only on the first PC; the resulting cube positions are then repeated across every component 1, ..., M to form the corresponding groups of cubes.

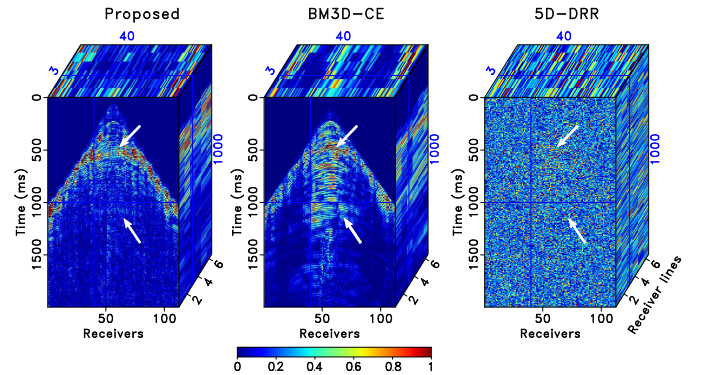


Fig. 3. Three-dimensional absolute differences between the original shot gather 4 and those interpolated by the proposed, BM3D-CE, and 5D-DRR methods. Note that the slices are at 1000 ms, receiver 40, and receiver line 3, respectively.

direction, where for each receiver line, cubes of dimension $L \times N \times M$ are configured. Our results were compared with those obtained by the competitive BM3D-CE [9] and 5D-DRR [17] methods. The root-mean-square error (RMSE) is used as the objective metric to assess the accuracy of the interpolated 3-D shot gathers. The method's parameters are tuned to minimize the RMSE; in particular, for the proposed method, we tuned the noise variance assumed by BM4D (σ_k , fixed for all k for simplicity) and the regularization parameters in (3) (λ , β) via the grid search tool from [27], obtaining values $\sigma_k = 10^{-5}$, $\beta = 8 \cdot 10^{-3}$, and $\lambda = 10^{-4}$. For 5D-DRR, the missing data was initialized with a spline interpolation. Furthermore, following [17], we used the *denoising and interpolation* mode of 5D-DRR with rank = 24 to account for the nonlinear seismic events.

Table I summarizes the interpolation results of the missing 3-D shot gathers 4, 6, and 9 in terms of average RMSE over the six receiver lines within each single interpolated 3-D shot gather, as well as over all 18 receiver slices in the three 3-D shot gathers, along with the corresponding standard deviation. The proposed method shows a better performance in all interpolated 3-D shot gathers. We also report the corresponding run times on an AMD Ryzen 7 5800X3D CPU on a single core and 128 GB RAM. The proposed method is highly efficient, also thanks to the PCA which allows to alleviate the computational burden of the cube-matching, evaluated only

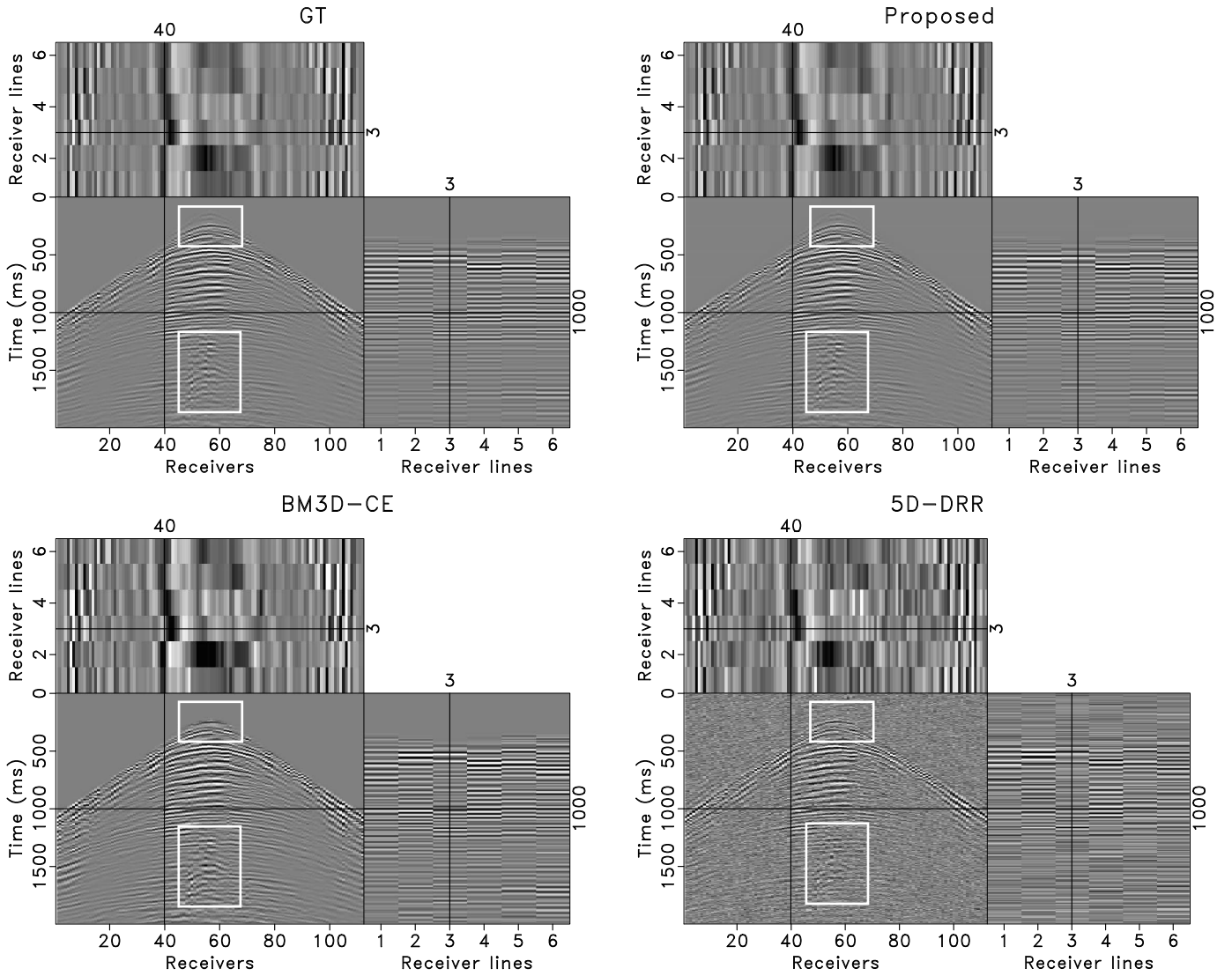


Fig. 4. Comparison of the interpolated 3-D shot gather 4 using the slices at time 1000 ms, receiver 40, and receiver line 3. The white box highlights the ground roll accurately reconstructed by the proposed method. The upper box shows the first arrivals omitted by the BM3D-CE method.

TABLE I
RMSE SUMMARY FOR THE MISSING 3-D SHOT GATHERS 4, 6, AND 9 INTERPOLATED BY THE PROPOSED METHOD, BM3D-CE [9], AND 5D-DRR [17]

Shot index	Proposed	BM3D-CE	5D-DRR
4	0.005 $\pm$ 0.001	0.035 $\pm$ 0.005	0.172 $\pm$ 0.007
6	0.004 $\pm$ 0.002	0.026 $\pm$ 0.007	0.194 $\pm$ 0.013
9	0.005 $\pm$ 0.001	0.043 $\pm$ 0.008	0.203 $\pm$ 0.019
{4, 6, 9}	0.0046 $\pm$ 0.0015	0.0346 $\pm$ 0.006	0.1896 $\pm$ 0.0130
Run time	1330 s	6600 s	2600 s

once on the first PC, instead of performing it separately on each channel. The low errors are visualized in Fig. 3, where the proposed method presents localized high errors near the linear events of the first arrivals primarily due to slight changes in the reconstructed amplitude, in contrast to the BM3D-CE method that concentrates its highest errors in the central part of the shot gather due to poor reconstruction of the ground roll in both amplitude and shape pointed with the arrows.

Fig. 4 provides a visual comparison of the 3-D shot gather 4 interpolated by the different methods. This visual inspection

confirms the results in the table, and it can be observed that BM3D-CE fails to interpolate internal seismic structures such as linear events related to the first arrivals and that 5D-DRR recovers the structures, but is highly contaminated with noise. Overall, our method provides a better reconstruction of seismic amplitudes and a smoother lateral continuity for seismic events including coherent noise. We evaluated the reconstruction quality of the different methods by extracting receiver 40 from shot gather 4 of the receiver line 3, as illustrated in Fig. 5. The analysis window ranges from 1240 to 1400 ms, and it is evident that the proposed method provides accurate alignment with all measurement points, especially in regions with high curvature. In contrast, the BM3D-CE method exhibited incorrect amplitude estimation of the waveform in these areas.

We finally note that, as reported by [9], the sparsity prior helps in the recovery of the low-frequency components of the shot gathers and the estimation with only the denoising regularization (i.e., $\lambda = 0$) also leads to inferior results due to the complexity of shapes related with nonlinear seismic events. As already commented, the PCA is beneficial for

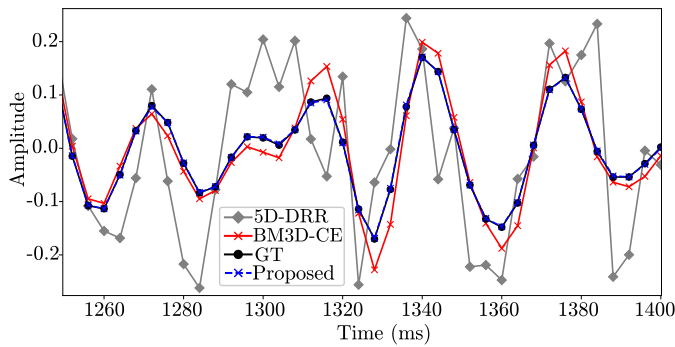


Fig. 5. Detailed waveform between 1240 and 1400 ms located on receiver 40, shot gather 4, and receiver line 3. The proposed method achieves the best fitting, especially in areas with higher curvature.

improving the matching and thus the sparsity, as well as for decreasing complexity; in particular, if each shot gather had been processed independently by (single-channel) BM4D, the RMSE and run time would approximately increase by 20% and 50%, respectively.

V. CONCLUSION

This letter proposes to employ a volumetric denoising regularizer and sparsity prior to 3-D shot-gather interpolation sampled simultaneously in several receiver lines. Because reflections always occur over a finite set of reflectors at depth and some seismic characteristics are repeated in the swath seismic acquisition, the proposed method exploits multichannel collaborative filtering of similar seismic volumes to improve the interpolation of typical 3-D events. Experimental results on the *Stratton 3-D survey* dataset showed the advantages of the proposed approach compared with leading competitive methods in a scenario of 3-D missing shots. Particularly, our approach provides lower RMSE and superior quality in the recovery of both linear and nonlinear seismic events and with less computational time.

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